

# NALANDA COLLEGE - COLOMBO 10 Grade11 Mathematics Third Term Unit Test

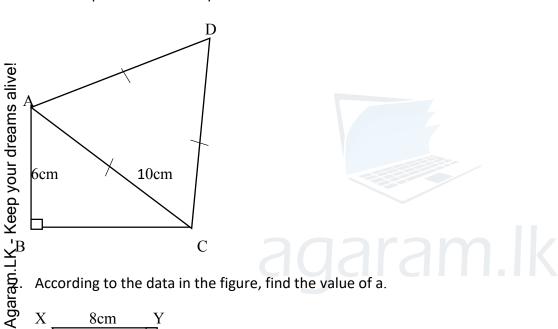
## 17) Pythagoras' Theorem

## <u>Part I</u>

1. Find the perimeter of the quadrilateral ABCD.

15cm

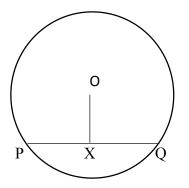
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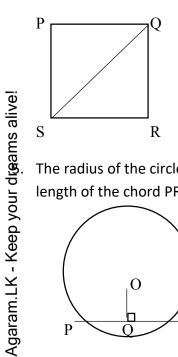


3. In the circle with the centre O, PQ is a chord. If PQ=6cm and OX=4cm find the radius of the circle.

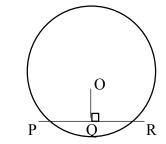




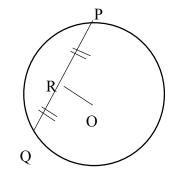
4. PQRS is a square, if the length of diagonal SQ is  $6\sqrt{2}$  cm find the area of the square.



The radius of the circle with centre O is 15cm. OQ is the perpendicular to the chord PR from O. OQ=9cm. Find the length of the chord PR.



6. In the circle with centre O, the length of the chord PQ is 10cm. PR=RQ and OR=12cm. Find the radius of the circle.

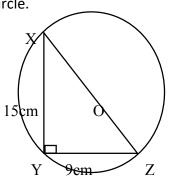






7. X,Y and Z are three points on the circle with the centre O. XY=15cm and YZ=9cm. Find the radius of the circle.





8. ABC is a triangle with  $A\hat{B}C$  a right angle. Show that  $AC = \sqrt{5} x$  cm.

8cm

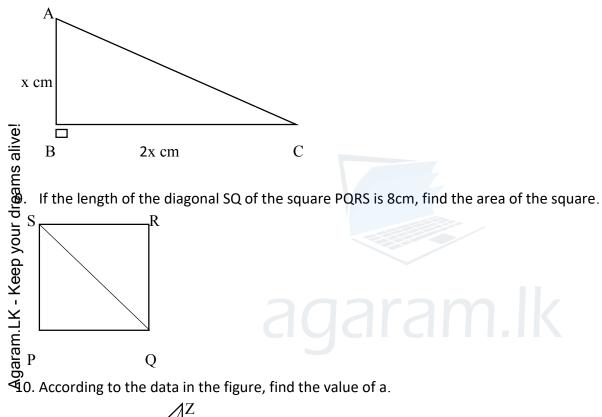
Y

10cm

P

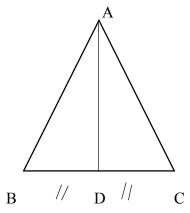
9cm

Х

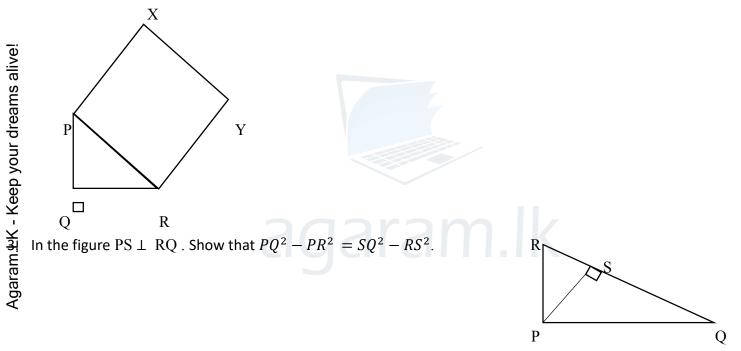




1. ABC is a equilateral triangle, D is the midpoint of BC. Show that  $4AD^2 = 3BC^2$ .



PQR is a right angled triangle and PRYX is a square. If PQ=QR, Show That,
 4 area of the triangle PQR = Area of the square PRYX





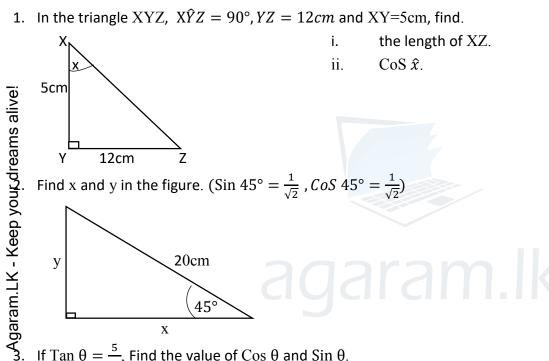




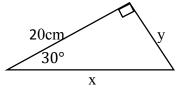
# NALANDA COLLEGE - COLOMBO 10 Grade11 **Mathematics Third Term Unit Test**

## 18) Trigonometry

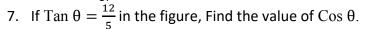
## Part I

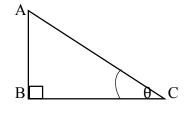


- If Tan  $\theta = \frac{5}{12}$ , Find the value of Cos  $\theta$  and Sin  $\theta$ .
- 4. The angle of elevation of the top of a vertical tree 18m from its foot is  $60^{\circ}$ . Find the height of the tree (Tan  $60^{\circ}$  = 1.732)
- 5. Find the value of x and y in the figure. (Sin  $30^{\circ} = 0.5$ , CoS  $30^{\circ} = 0.8660$ , Tan $30^{\circ} = 0.5774$ )



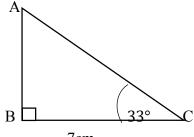
6. If  $\sin \theta = \frac{8}{17}$ , Find the value of  $\operatorname{Tan} \theta$ .







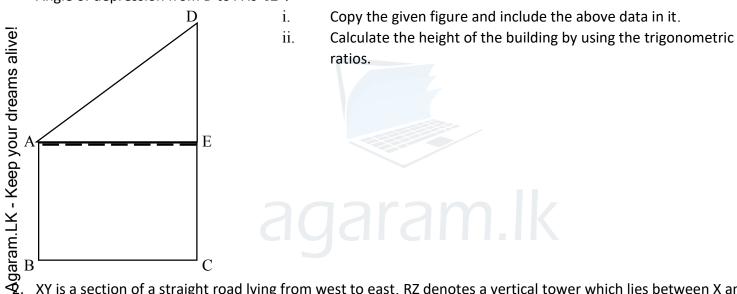
- 8. A wire attached to a ring at the top of a lamp post is attached to a point on the ground distance 40m its foot. The angle between the wire and the ground is  $45^\circ$ . Find the length of the wire. (*Cos*  $45^\circ = 0.7071$ )
- 9. In the triangle ABC,  $A\hat{C}B = 33^\circ$ , BC = 7cm. Find the length of AB. ( $Tan 33^\circ = 0.6494$ ).



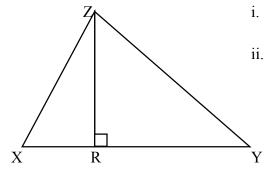
7cm 10. If  $\cos \theta = \frac{9}{15}$ , Find the value of Tan  $\theta$ .

#### <u>Part II</u>

 The given sketch shows building CD and 4.2m height tree AB are situated on a horizontal ground at distance 50m. Angle of depression from D to A is 42°.



 XY is a section of a straight road lying from west to east. RZ denotes a vertical tower which lies between X and Y. The angle of elevation of Z from X is 42°. XR=50m.



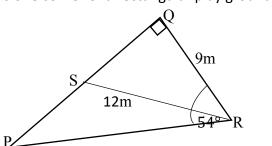
Find the height of RZ to the nearest meter using trigonometric ratios.

If YZ=150m, find the angle of elevation of Z when observed from Y.

3. Q is one corner of a rectangular play ground. The point R is located along one boundary of the ground 9m from Q.

i.

ii.



The point P is located along another boundary of the ground Such that  $Q\hat{R}P = 54^{\circ}$ . Find the distance PQ to the nearest meter. The point S is located on PQ, 12m away from R. Calculate the magnitude of  $Q\hat{R}S$ .





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#### 19) Matrices

Part I 1. If  $A = \begin{bmatrix} 2 & -1 \\ 3 & 4 \end{bmatrix}$  and  $B = \begin{bmatrix} -2 & 4 \\ -3 & 1 \end{bmatrix}$ , find A+B. 2. Simplify.  $\begin{bmatrix}
3 & 4 \\
2 & -1 \\
0 & 5
\end{bmatrix}
\begin{bmatrix}
-2 & 3 \\
5 & 7 \\
-3 & -2
\end{bmatrix}$ Find the matrix A. Find the matrix A. If  $\begin{bmatrix} 4 & -1 \\ 3 & 5 \end{bmatrix} - A = \begin{bmatrix} 4 & -3 \\ 9 & 2 \end{bmatrix}$ , Find the matrix A. If  $A = \begin{bmatrix} 2 & 3 \\ 1 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} -1 & -2 \\ 3 & 1 \end{bmatrix}$ , Find 2A+3B. Find PQ. If  $P = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$  and  $Q = \begin{bmatrix} 2 & -1 \\ 3 & 4 \end{bmatrix}$ , Find PQ. B. P = \begin{bmatrix} 4 & -1 \\ 3 & 2 \end{bmatrix} and  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  find the matrix Q such that 2P+Q=I. If  $X = \begin{bmatrix} 4 & 3 \\ -1 & -2 \end{bmatrix}$  and  $Y = \begin{bmatrix} 5 & -3 \\ 2 & -4 \end{bmatrix}$ , find the 2X+Y. By B. If A =  $\begin{bmatrix} 4 & 3 \\ -2 & 1 \end{bmatrix}$  and B =  $\begin{bmatrix} -2 & 4 \\ -1 & 3 \end{bmatrix}$ , find AB. 9. Simplify.  $\begin{bmatrix} 3 & -1 \\ 4 & 7 \\ 2 & 1 \end{bmatrix} - \begin{bmatrix} 4 & -5 \\ 3 & 0 \\ 2 & 6 \end{bmatrix}$ 10. If  $3X+2\begin{bmatrix} 7\\ -3 \end{bmatrix} = \begin{bmatrix} 5\\ -3 \end{bmatrix}$  Find X.

#### <u>Part II</u>

1. i) If 
$$X = \begin{bmatrix} 3 & a \\ 2b & 2 \end{bmatrix}$$
, write the matrix 3X.  
ii) Find a and b such that  $3X + \begin{bmatrix} 3 & 1 \\ 8 & a \end{bmatrix} = \begin{bmatrix} 12 & 4 \\ 14 & 7 \end{bmatrix}$ .  
iii) Find the matrix  $\begin{bmatrix} -8 & 3 \\ 7 & 4 \end{bmatrix} - 2X$ .



2. If 
$$A = \begin{bmatrix} 4 & -2 \end{bmatrix}$$
,  $B = \begin{bmatrix} 3 \\ -1 \end{bmatrix}$ ,  $C = \begin{bmatrix} 1 & 3 \\ -1 & 2 \end{bmatrix}$  and  $D = \begin{bmatrix} -4 & 2 \\ 5 & -1 \end{bmatrix}$ . Find,  
i) 2C+D  
ii) AB  
iii) CB

3. i) Write the matrix P, if P + Q = 
$$\begin{bmatrix} 4 & 3 & -1 \\ 5 & 2 & 1 \end{bmatrix}$$
 and Q =  $\begin{bmatrix} -2 & 3 & 4 \\ -1 & 5 & 2 \end{bmatrix}$ 

ii) If 
$$X = \begin{bmatrix} 4 & -3 \\ 1 & 2 \end{bmatrix}$$
 and  $Y = \begin{bmatrix} -2 & -3 \\ 5 & -2 \end{bmatrix}$ , Find,  
a)  $X + 2Y$   
b)  $XY$ 

iii) If  $A = \begin{bmatrix} 4 & 1 \\ -2 & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} -3 & 5 \\ 4 & -1 \end{bmatrix}$  Find the matrix C, such that A - B - C = 0



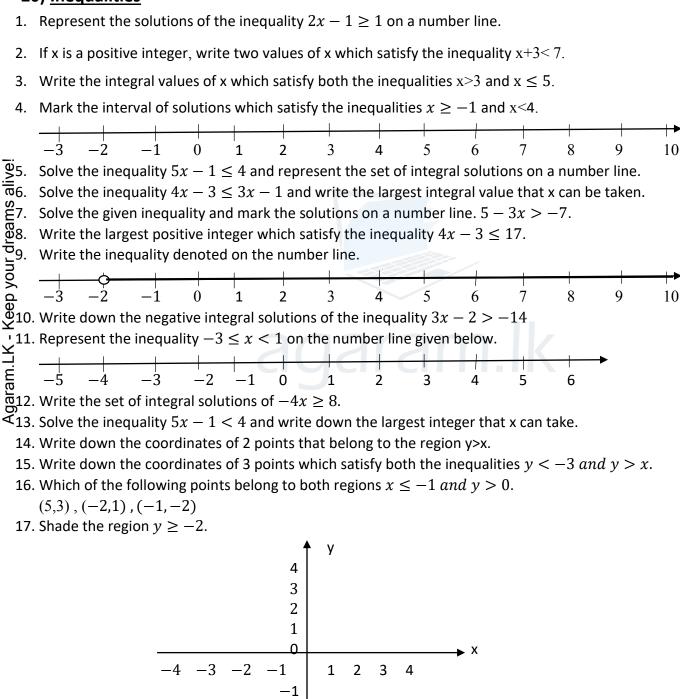


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#### 20) Inequalities



-2 -3 -4

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www.agaram.lk 18. Sunil has Rs.300. He bought 4 apples at the rate of Rs.x each and 3 oranges at the rate of Rs.40 each. Build up an inequality for this information and find out the maximum price of an apple.



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- 19. Find the minimum whole number value of x that satisfies the inequality 5x 3 > 3x + 1.
- 20. Amal bought 6 Rambutans at Rs.x and 6 toffees at Rs.3 each. Sunil bought 3 Rambutans at Rs.x each and 6 toffees at Rs.4 each. If the amount spent by Amal is more than or equal the amount Sunil spent, what is the minimum price of a Rambutan?





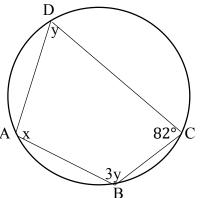


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## 21) Cyclic Quadrilaterals

## <u>Part I</u>

1. ABCD is a cyclic quadrilateral. Find the values of x and y.

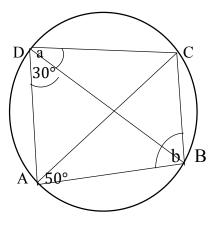


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In the diagram, the vertices of the quadrilateral PQRS lie on a circle with centre O. Find the value of x.



3. ABCD is a cyclic quadrilateral. Find the values of a and b.

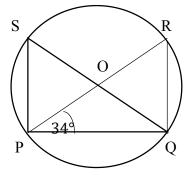




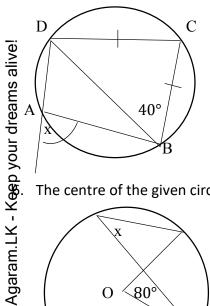


4. In the circle with centre O shown in the figure,  $R\hat{P}Q = 34^{\circ}$  Find the magnitude of  $P\hat{S}Q$ .

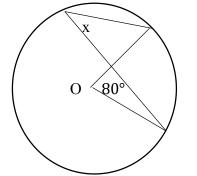




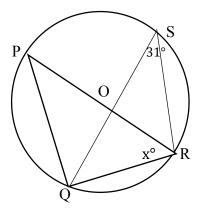
In the figure ABCD is a cyclic quadrilateral. Find the value of x. 5.



The centre of the given circle is O. Find the value of x.



7. O is the centre of the circle in the figure. Find the value of x.



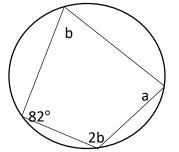


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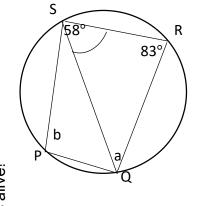
8. Find the angles marked by symbols.

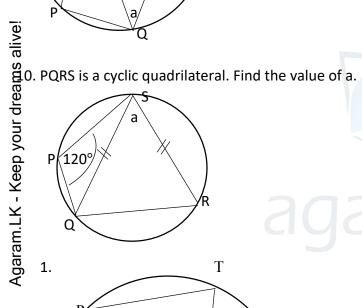


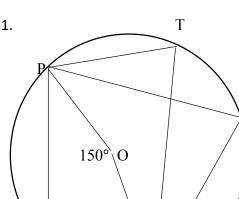
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9. PQRS is a cyclic quadrilateral. Find the value of a and b.



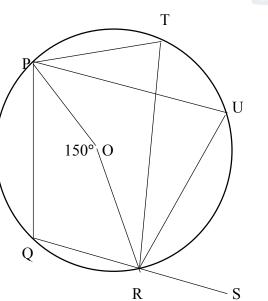




Part II

According to the data in the figure,

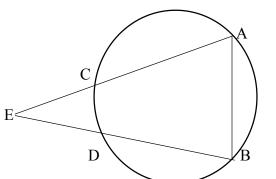
- Find the value of  $P\hat{T}R$ . i.
- Find the value of  $P\hat{Q}R$ . ii.
- Name an angle equal to angle  $P\widehat{U}R$ . iii.
- Name an angle equal to angle  $U\hat{R}S$ . iv.
- By giving reasons name an angle equal to angle  $T\hat{R}S$ . v.





i.

In the cyclic quadrilateral ABDC, AC an BD produced meet at E. If AE=BE, 2.



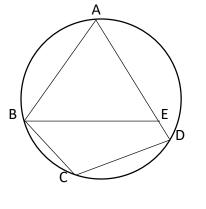
Show that CDE is an isosceles triangle.



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ii. Prove that AB//CD.

In the cyclic quadrilateral ABDC. AB=BE. Show that  $B\hat{E}D = B\hat{C}D$ 3.

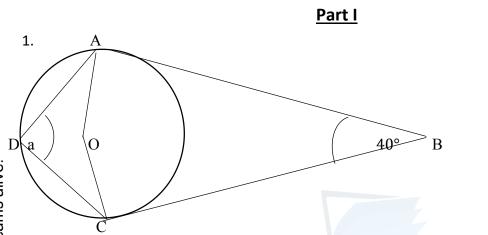






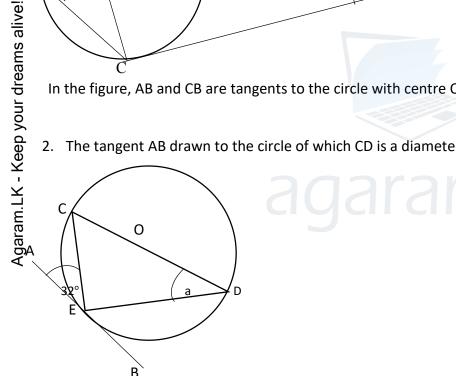
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## 22) Tangents

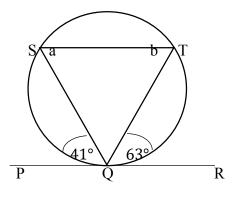


In the figure, AB and CB are tangents to the circle with centre O. Find the value of a

2. The tangent AB drawn to the circle of which CD is a diameter, touches the circle at E. Find the value of a.



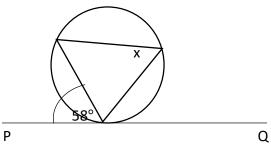
3. In the figure PR is a tangent at Q. Find the values of a and b.



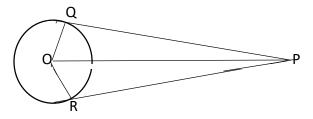


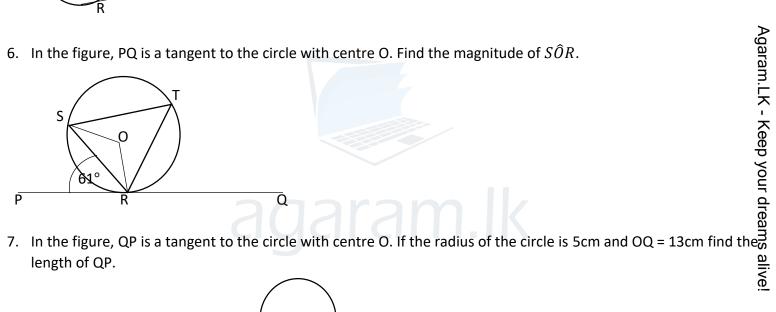


4. PQ is a tangent to the circle. Find the value of x.

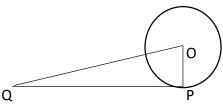


5. PQ and PR are two tangents drawn to the circle with centre O, from external point P. If  $Q\hat{P}O = 24^{\circ}$ , Find the magnitude of  $Q\hat{O}R$ .

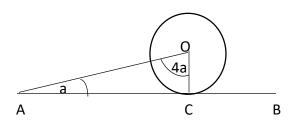




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8. In the figure, AB is a tangent to the circle with centre O. Find the magnitude of  $A\hat{O}C$ .

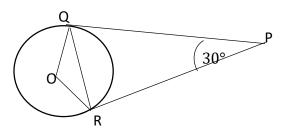




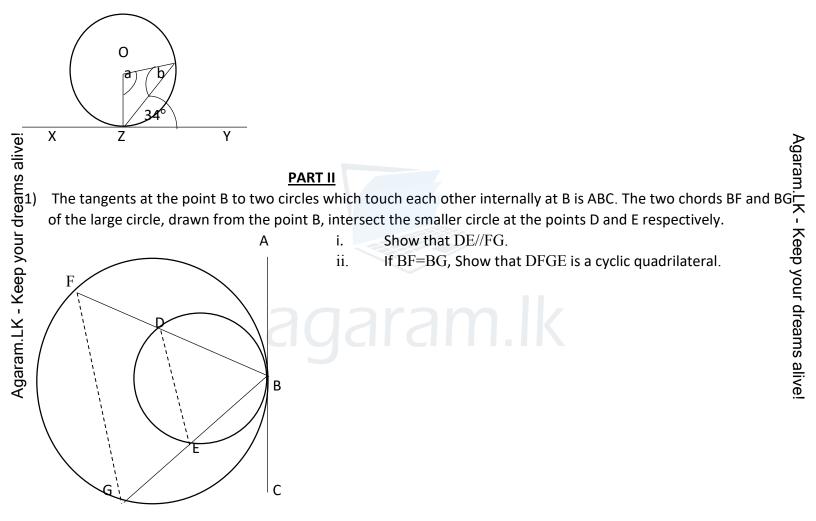


9. In the figure PQ and PR are tangent to the circle with centre O. Find the magnitude of  $P\hat{R}Q$ .

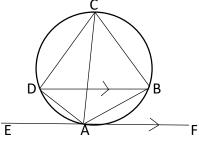




10. In the figure XY is a tangent at Z. O is the centre of the circle. Find the values of a and b.



2) In the given diagram, ABCD is a cyclic quadrilateral. The tangent drawn to the circle at A is EF.



- i. Name an angle equal to  $B\hat{A}E$ . Give reasons for your answer.
- ii. Show that  $D\hat{C}A = B\hat{C}A$
- iii. Show that AB = AD.



www.agaram.lk If AC is a diameter of the circle, AB = x cm and BC = 2AB, show that the diameter of the circle iv. is  $\sqrt{5} x cm$ .

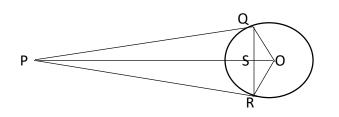


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- 3) In the figure PQ and PR are tangents to the circle with centre O.
  - $P\hat{Q}S = P\hat{R}S$ Show that, i)

QS = SRii)

PQOR is a cyclic quadrilateral. iii)







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**Mathematics** 

**Third Term** 

**Unit Test** 



## 23) Constructions

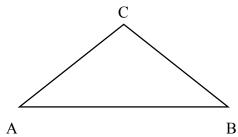
## Part I

1. The location of a point X which lies on AB, and equidistant to AC and BC is needed to be marked, By showing the relevant construction lines mark the location of X.

A and B are two fixed points. The point C moves such that the area of the triangle ABC is constant. Express the locus of point C with a diagram.

A sphere of radius 6cm rolled along a straight plane surface. Express the locus of the centre of the sphere with a diagram.

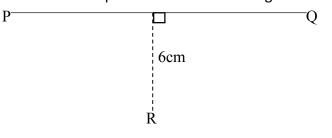
Agaram.LK - Keep your dreams alive! In the triangle ABC shown in the figure, draw a sketch of the construction lines required to locate the point D on AB such that DB=DC.



B

5. Draw a clear sketch of the construction lines required to find the vertices S and T which are on PQ and 8cm apart from R. Mark the points S and T on the diagram.

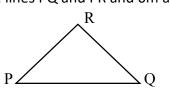
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6. In the given diagram draw a sketch of relevant construction lines to locate a point S, which is equidistant to the lines PQ and PR and 6m away from P.



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- 7. Two mango trees X and Y are situated 15m away from each other. A rambutan tree "Z" is needed to be plant equidistant to X and Y and 10m away from X. Using the knowledge of loci draw a rough sketch and show that there exist two points for Z.
- 8. It is needed to find the point X, which is equidistant to the three sides of the triangle PQR. An incomplete sketch drawn for that is given below. Complete the figure and mark the location of X.



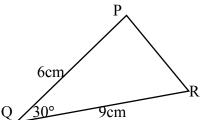
p\_

Sketch a construction to find the centre of the given arc. construction lines obtain the locations of the vertices S and Q of the rhombus.

- R

Part II

1. Use only a straight edge with a cm/mm scale and a pair of compasses to the following constructions. Draw your construction lines clearly.



- i. Construct the given triangle PQR.
- ii. Construct a perpendicular from P to QR and name the point it meets QR as S.
- iii. Construct the circle that passes through the points P, R and S.



iv. Construct the tangent to this circle at the point R, and name the point at which it meets PS produced as T.



- 2. Using only a straight edge with a mm/cm scale and a pair of compasses, and indicating the lines of construction clearly.
  - i. Construct  $P\hat{Q}R$  such that PQ=8cm,  $P\hat{Q}R = 30^{\circ}$  and QR = 6cm.
  - ii. Obtain the location of S which lies at equal distance from Q and R and is such that  $P\hat{Q}S = 90^{\circ}$ .
  - iii. Construct the circle that has S as its centre and SQ as its radius.
  - iv. Produce QS and name the point of intersection of that line and circle as T.
  - v. By giving reasons find the value of  $Q\hat{T}R$ .
- 3. Using only a straight edge with a cm/mm scale and a pair of compasses, and showing the construction lines clearly;
  - i. Construct a straight line segment PQ of length 9cm.
  - ii. Construct the perpendicular bisector of PQ.
  - iii. Obtain the location of R such that PR=7cm and  $P\hat{R}Q = 90^{\circ}$ .
  - iv. Measure and write down the length of QR.
  - v. Construct a straight line parallel to PQ through R.
  - vi. Find the location of point S on this line such that  $R\hat{P}Q = R\hat{S}Q$ .
  - vii. Giving reasons, find  $P\hat{S}Q$ .

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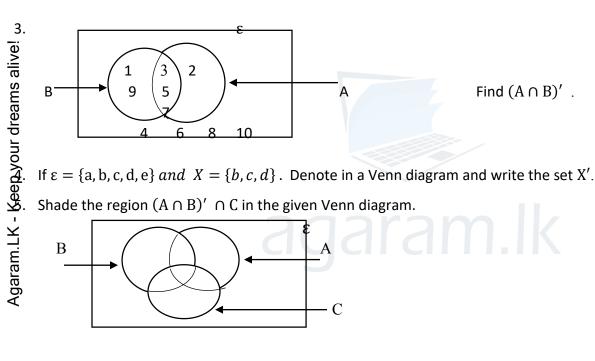


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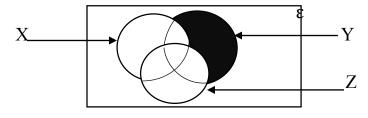
## 24)<u>Sets</u>

## <u>Part I</u>

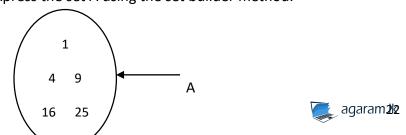
- 1. If n(A) = 40, n(B) = 60 and  $n(A \cap B) = 42$ , Find  $n(A \cup B)$ .
- 2. If  $\varepsilon = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$  and  $X = \{2, 4, 6, 8, 10\}$  Find X'.



6. Write down the shaded region in the Venn diagram using set notation.

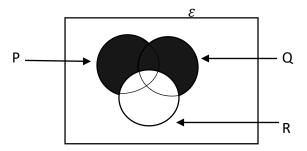


- 7. If  $\varepsilon = \{1,3,5,7,9\}$  and A = {5}. Denote it on a Venn diagram and write the set A'.
- 8. If  $\varepsilon = \{a, b, c, d, e, f\}$ , A = {a,b,c} and B={b,c,d} find  $A \cap B$ .
- 9. Express the set A using the set builder method.



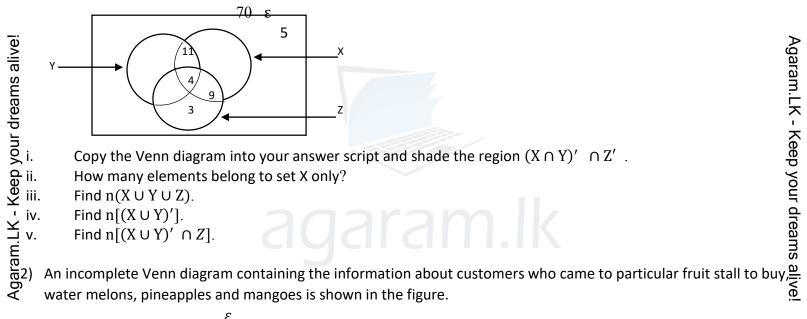
10. Write the set notation, the region shaded in the Venn diagram.

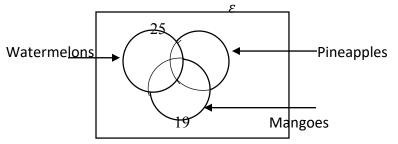




#### Part II

1. These sets X, Y and Z belonging to the universal set  $\varepsilon$  are shown in the Venn diagram n(X)=34, n(Y)=32 and  $n(\epsilon) = 70$ .





The number of people who bought water melons and mango is 7, two of them did not buy pineapples.

The number of people who bought only pineapples is 8 while 12 bought pineapples and mangoes.

5 bought only water melons. Everyone who comes to the fruit stall buys at least one fruit.

- i. Represent this information in the given Venn diagram.
- ii. How many bought only water melons and pineapples?
- iii. How many bought only mangoes?
- Find the total number of customers who came to the fruit stall. iv.



3) 
$$\varepsilon = \{a, b, c, d, e, f, g, h, i, j, k, l, m\}$$
  
 $A = \{e, f, g, h, i, j\}$   
 $B = \{g, h, i, j\}$   
 $C = \{e, k, l\}$ 

- i. Represent the given sets in a Venn diagram.
  - Find, a)  $(A \cap B)$

ii.

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- b)  $(A \cup B) \cap C$
- c)  $(A \cup B \cup C)'$
- iii. Shade the region  $(A \cap B)' \cap C$  in the Venn diagram.







# NALANDA COLLEGE - COLOMBO 10 Grade11 **Mathematics Third Term Unit Test**

## 25) Probability

5

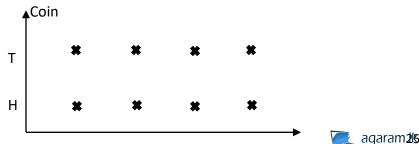
### Part I

- 1. A cubical die with its faces marked 1,2,3,4,5 and 6 is rolled twice. By considering the numbers on the faces that touch the table, represent all the possible outcomes on a grid.
- There are 4 identical blue beads and 3 red beads in a bag. Find the probability of randomly selected bead being.
  - i. A white bead,
  - ii. A red bead.
- Find the probability of obtaining a number greater than 2, when rolling a tetrahedral die marked 1 to 4 on its faces.

Agaram.LK - Keep your dreams alive! بې A tree diagram related to the selection of a pen, taken out randomly from a bag containing blue and black pens is given in the figure. Find the probability of obtaining a black pen.

Obtaining a blue pen

- Obtaining a black pen
- 5. Find the probability of obtaining a composite number, when rolling an unbiased die marked 1 to 6 on its faces.
- 6. If the probability of occurring an event X is  $\frac{3}{r}$ , what is the probability of not occurring the event X is?
- 7. When two, five-rupee coins are tossed simultaneously, find the probability that at least one coin shows tail.
- 8. For the events X and Y of a random experiment.  $P(X) = \frac{3}{7}$ ,  $P(Y) = \frac{2}{7}$  and  $P(X \cap Y) = \frac{1}{14}$ . Find  $P(X \cup Y)$ .
- 9. There are 8 identical cards numbered from 1 to 8 in a box. A card is taken form the box randomly. Find the probability of getting a prime number.
- 10. If an unbiased coin and a tetrahedral die are tossed, possible outcomes are denoted on the given grid. Find the probability of an even number on the die and tails on the coin.



#### www.agaram.lk Die

2 3 Δ

#### **PART II**

- 1) In a competition of shooting at a target, the probability of shooting at a target for a particular competitor is  $\frac{5}{2}$ .
  - Succeed

1

5

. . . . . . . . . . .

 $\mathbf{\Sigma}$ 

i.

Not succeed

- i. Complete the given incomplete tree diagram.
- ii. If he shoots twice at the target, extend the given tree diagram in a suitable way.
- iii. Find the probability of the following events.
  - a) He succeeds in both attempts
  - He succeeds only in one attempt b)
  - c) He does not succeed in any of the two attempts.

- Keep your dreams alive! There are 9 mangoes of the same size in a bag. 5 of them are raw and rest are ripe. One mango is drawn from the bag and observed whether it is raw or ripe, and without replacing the first one, another mango is drawn and observed.

- Denote the sample space of the above experiment on a grid.
- ii. Find the probability that the first mango drawn is ripe.
- iii. Find the probability that the second mango drawn is raw.
  - Find the probability that both mangoes are raw.

The boxes P and Q contain identical balls. Box P has 3 blue balls and 4 white balls. The box Q has 2 blue balls and 3 Agaram white balls. A ball is taken out at random from bag P and put into bag Q and then a ball is taken out at random from bag Q.

- Represent the sample space relevant to this experiment in a tree diagram.
- ii. Find the probabilities of the following events.
  - The ball taken from Q is a blue ball
  - b) The ball taken from P is a white ball



